## Chemical Kinetics

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## A BRIEF HISTORY OF CHEMICAL KINETICS

Ref: "The World of Physical Chemistry," by K. J. Laidler, Oxford Univ. Press, 1993)
-1850: Wilhelmy (Germany) studied the rate of inversion of sucrose (hydrolysis into D-(+)-glucose and $D-(-)$-fructose in the presence of an acid) and found it to be proportional to the concentrations of both the sugar and the acid.
-1864: Guldberg and Waage (Norway) formulated their "law of mass action," according to which the reaction "forces" are proportional to the product of the concentrations of the reactants: $\mathrm{K}=[\mathrm{R}]_{r}[\mathrm{~S}]_{\mathrm{l}} /\left([\mathrm{A}]_{a}[\mathrm{~B}]_{\mathrm{b}}\right)$ where $\mathrm{a}, \mathrm{b}$, r and s are the stoichiometric coefficients in the chemical equation $A+B=R+S$. So the rate of the forward reaction is proportional to $[A]_{a}[B]_{b}$ and that of the reverse reaction is proportional to $\{\mathrm{R}] \mathrm{r}[\mathrm{S}]$ s.
-1865-67: Harcourt and Esson (UK) analyzed the reactions between $\mathrm{H}_{2} \mathrm{O}_{2}$ and HI and between $\mathrm{KMnO}_{4}$ and $(\mathrm{COOH})_{2}$. They wrote the corresponding differential equations, integrated them and determined the concentration vs. time relationships. They also proposed an equation for the temperature dependence of the reaction rate, $\mathrm{k}=\mathrm{A}$ Tc. Mathematical expressions.
-1884: van't Hoff (The Netherlands) published his "Studies of Chemical Dynamics" (Études de dynamique chimique), in which he generalized and further developed the work of Wilhelmy, Harcourt and Esson. In particular, he introduced the differential method of analysis. He also analyzed the temperature dependence of the equilibrium constant (now called the "van't Hoff equation") and of forward and reverse reaction rates.
-1887: Ostwald (Germany; Latvia) introduces the terms "reaction order" and "half-life" in his "Lehrbuch der allgemeinen Chemie."
-1889: Arrhenius (Sweden) further analyzed the temperature dependence of reaction rate, $\mathrm{k}=\mathrm{A}$ $\exp (-B / T)$, and gave it an "energy barrier" interpretation; this is now called the "Arrhenius equation."

Kinetics refers to a branch of mechanics dealing with the motion of particles without considering any external forces acting on the particles. This differs from dynamics which takes into account of the external forces acting on the particles.

In the gas phase, chemical kinetics can be treated in terms of the kinetic theory of gases and the statistical mechanics of isolated atoms. In the liquid phase, the molecules are closer and applications of molecular theories are difficult. In the liquid phase, many reactions are diffusion controlled and the rate constants depend upon the rate with which the reactants can diffuse together.

Chemical reactions occur at a definite rate.
Slow... Fast....in kinetics.
One is concerned with reactions in-between.
Some of them are very slow...

Neutralisation of an acid by alkali in aqueous solution.... fast

## Diamond to graphite... slow



Rate of a chemical reaction depends upon the concentration of the reacting substances. In the gas phase, it depends upon the pressure. Since the concentration is decreasing steadily, the rate decreases. A variation of rate with time is shown in the figure.

$\mathrm{N}_{2} \mathrm{O}_{5} \rightarrow \mathrm{~N}_{2} \mathrm{O}_{4}+\mathrm{O}_{2}$

The rate depends only on the concentration of $\mathrm{N}_{2} \mathrm{O}_{5}$ except at very low pressures.
$\mathrm{RCOOR}^{\prime}+\mathrm{H}_{2} \mathrm{O} \rightarrow \mathrm{RCOOH}+\mathrm{R}^{\prime} \mathrm{OH}$
Although both ester and water are involved in the reaction, the concentration of water does not undergo any significant change during the reaction. Thus the reaction is first order although there are two reacting species.

Dissociation of HI is second order.
Reaction of NO and $\mathrm{O}_{2}$ giving $\mathrm{NO}_{2}$ is third order depending on the square of the NO concentration and the concentration of $\mathrm{O}_{2}$.

$$
\begin{aligned}
& \text { Rate }=\mathrm{k}_{1}{ }_{1} 11 C_{2}{ }^{\mathrm{n} 2} \mathrm{C}_{3}{ }^{\mathrm{n} 3} \ldots \\
& \text { The overall order } \mathrm{n} \text { is } \\
& \mathrm{n}=\mathrm{n} 1+\mathrm{n} 2+\mathrm{n} 3+\ldots
\end{aligned}
$$

Rate constant

The reaction is of order n 1 in reactant 1 , and n 2 in reactant 2 , etc. It may appear that any order is possible, but in reality order does not exceed three.

Chemical reactions can be classified in terms of the molecularity. This number is the number of molecules or atoms taking part in each act of chemical reaction.

The dissociation of nitrogen pentoxide is a unimolecular reaction.
This can occur in the gaseous or solution phase.
$\mathrm{N}_{2} \mathrm{O}_{5}=\mathrm{N}_{2} \mathrm{O}_{4}+1 / 2 \mathrm{O}_{2}$
In HI dissociation, two molecules take part.
$2 \mathrm{H}_{1}=\mathrm{H}_{2}+\mathrm{l}_{2}$
The reaction is not, $\mathrm{HI}=1 / 2 \mathrm{H}_{2}+1 / 2 \mathrm{I}_{2}$
Another biomolecular reaction is
$\mathrm{CH}_{3} \mathrm{COOC}_{2} \mathrm{H}_{5}+\mathrm{H}_{2} \mathrm{O}=\mathrm{CH}_{3} \mathrm{COOH}+\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}$

If three molecules are involved, the overall process is termolecular. $2 \mathrm{NO}+\mathrm{O}_{2}=2 \mathrm{NO}_{2}$

In simple reactions, the number of reactants appearing in the stoichiometric reaction is the molecularity. However, reactions can occur in multiple steps referred to as elementary processes. Molecularity can be assigned to each individual step, which indicates the species reacting in that step. This form of assignment is possible only if the mechanism is known.

Molecularity is concerned with the mechanism. But the order of a reaction expresses the dependence of measured rate on the concentration of the reactants.

Order and molecularity can be same or different. In reactions where one of the reactant is present in large excess, this is invariably the case. Order of a reaction can be zero and even fractional, but molecularity is never zero and always an integer. The decomposition of gaseous acetaldehyde has been shown to have an order of $3 / 2$. The reaction of $\mathrm{H}_{2}$ and $\mathrm{Br}_{2}$ to from HBr has a rate proportional to $\left(\mathrm{Br}_{2}\right)^{1 / 2}$ in the absence HBr and $(\mathrm{Br} 2) 3 / 2$ in the presence of sufficient amount of HBr . The rate of formation of phosgene $\left(\mathrm{COCl}_{2}\right)$ from CO and $\mathrm{Cl}_{2}$ is given by $\mathrm{k}\left(\mathrm{Cl}_{2}\right) 3 / 2(\mathrm{CO})$. Order and molecularity are not completely independent, however. Measurements of order are sometimes used to confirm or contradict a proposed mechanism.

We shall consider only homogeneous, simple reactions taking place at a constant temperature.

How do you probe the system?
Physical and chemical methods
Physical method is preferred, no variation of concentration.
Pressure of a gas, the conductance of an electrolyte, extent of light absorption, rotation of polarisation of an incident light beam, extent of fluorescence of a species etc. are monitored.

In the chemical method, a small portion of the sample is taken form time to time, and the product concentration is analysed.

## First order reaction

In first order, rate is proportional to the concentration of one of the reactants.
$-d[C] / d t=k[C]$
[C] is the concentration of the reactant at time t . k is the proportionality constant or the rate constant or the velocity constant or the specific reaction rate.

When $[C]=1$ rate $=k$. Rate at any concentration $C$ is the product of $k$ and $[C]$.
In practice, it is advantageous to use the relation in a different form.
$-\mathrm{d}[\mathrm{C}][\mathrm{C}]=\mathrm{kdt}$
Upon integration,
$-\int \mathrm{C}_{\mathrm{co}} \mathrm{d}[\mathrm{C}] /[\mathrm{C}]=\mathrm{k} \int_{0}^{\mathrm{t}} \mathrm{dt}$
Where [C]o is the concentration of the reactant at time 0 and $[C]$ at time $t$
$\ln [\mathrm{C}] \mathrm{o} /[\mathrm{C}]=\mathrm{kt}$
$\mathrm{k}=1 / \mathrm{t} \ln [\mathrm{C}] \mathrm{o} /[\mathrm{C}]$
[C]o is proportional to a and [C] to a-x.
$k=1 / t \ln (a / a-x)$

## Important characteristics of the first order rate equation

Any unit of concentration could be used as long as both a and a-x are expressed in the same units. The specific reaction rate has unit of time-1 and is generally expressed as sec-1.

Important characteristic of a first order reaction is the time taken for the completion of a fraction the reaction. If 0.5 is the time required for the completion of half of the reaction,
$\mathrm{t}_{0.5}=(2.303 / \mathrm{k}) \log 2=0.693 / \mathrm{k}=\mathrm{t} 0.5$
This value is called the half-life, which is a constant for the reaction.
Time to complete any definite fraction of the reaction is constant.


The value of k can tell us quickly the rate at which products are formed.

## Examples of first order reactions

$\mathrm{N}_{2} \mathrm{O}_{5}(\mathrm{~g})=\mathrm{N}_{2} \mathrm{O}_{4}(\mathrm{~g})+1 / 2 \mathrm{O}_{2}(\mathrm{~g})$

For every mole of $\mathrm{N}_{2} \mathrm{O}_{5}$ decomposed, the number of moles of the system increases by $11 / 2$ in a constant volume apparatus, the partial pressure $x$ of $\mathrm{N}_{2} \mathrm{O}_{5}$ decomposed is equal to double the increase in gas pressure.

Measurement of pressure will not directly give the amount of $\mathrm{N}_{2} \mathrm{O}_{5}$ decomposed since $\mathrm{N}_{2} \mathrm{O}_{4}$ formed will undergo further decomposition to form $\mathrm{NO}_{2}$. This can however be accounted for by knowing the equilibrium constant of this reaction.

The measured rate constant is approximately constant at $1.3 \times 10-4$ sec-1 which shows that the reaction is first order.
$\mathrm{N}_{2} \mathrm{O}_{5}$ equilibrium has also been studied in solution. By keeping the appropriate solvents it is possible to keep $\mathrm{N}_{2} \mathrm{O}_{4}$ and $\mathrm{NO}_{2}$ formed in solution and the volume of oxygen evolved is measured. The amount of $\mathrm{O}_{2}$ produced corresponds to double the amount of $\mathrm{N}_{2} \mathrm{O}_{5}$ decomposed. The final $\mathrm{O}_{2}$ volume will give the value of $a$.

Instead of individual values of $k$, a graphical method can be employed.
$t=(2.303 / k) \ln a-(2.303 / k) \log (a-x)$
A plot of $t$ against $\log (a-x)$ should give a straight line with $-2.303 / k$ as the slope.

Another first order reaction.
$\mathrm{N}_{2} \mathrm{O}_{5}=\mathrm{NO}_{3}+\mathrm{NO}_{2}$
The hydrolysis of an ester is very slow if only water is present. In the presence of an acid catalyst, the reaction has a measurable rate. Hydrolysis of methyl acetate in presence of HCl is such a reaction. The concentration of acid is small and it does not change during the reaction. Water concentration is high and it does not change appreciably. Thus the rate depends only on the concentration of methyl acetate and the rate is first order. To follow the reaction, a small volume of the $r_{n}$ mixture is withdrawn at definite intervals and it is titrated against standard alkali. The volume of alkali consumed at time $0, \infty$ and t will give the rate constant of the reaction.
$k=2.303 / t \log \left(T_{\infty}-T_{0} / T_{\infty}-T_{t}\right)$
$T_{\infty}-T_{0}$ refers to $a . T_{t}-T_{0}$ is $x$.
Experimental studies show that k determined remains a constant. It has to be said that k does depend upon the amount of water and the concentration of acid. With these, the value of k will change.

Another example is the inversion of sucrose. This is also catalysed by acid. The course of the reaction can be measured by determining the angle of rotation of polarised light. Sucrose rotates it to right and a mixture of dextrose and laevulose makes it to left. If $\alpha_{0}$ and $\alpha_{\infty}$ and $\alpha_{t}$ are the angles of rotation including the sign, $\alpha_{0}-\alpha_{\infty}$ is proportional to a and $\alpha_{t}-\alpha_{\infty}$ is proportional to $a-x$.

Thus, $k=2.303 / t \log \left(\alpha_{0}-\alpha_{\infty} / \alpha_{t}-\alpha_{\infty}\right)$

Here again the value of k depends on the concentration of water and acid.
$\mathrm{C}_{12} \mathrm{H}_{22} \mathrm{O}_{11}+\mathrm{H}_{2} \mathrm{O}=\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}+\mathrm{C}_{6} \mathrm{H}_{12} \mathrm{O}_{6}$
Sucrose Dextrose Laevulose
A typical decomposition reaction is that of azomethane.
$\mathrm{CH}_{3} \mathrm{~N}_{2} \mathrm{CH}_{3}(\mathrm{~g}) \rightarrow \mathrm{CH}_{3} \mathrm{CH}_{3}(\mathrm{~g})+\mathrm{N}_{2}(\mathrm{~g})$
This reaction can be monitored by measuring the total pressure as a function of time. Since all the species are in the gas phase, the pressure is a direct measure of the concentration. This is depicted below.
The shape of the graph (logarithm of concentration is linear with time) illustrates that the reaction is first order.


## Second order reactions

The rate of a second order reaction depends upon two concentration terms. It can be
$2 A \rightarrow$ Products or
A + B $\rightarrow$ Products
$-d C_{A} / d t=k C_{A}^{2}$ or $-d C_{A} / d t=-C_{B} / d t=$
$k_{A} C_{B}$ In general,
$-\mathrm{dC} / \mathrm{dt}=\mathrm{k} \mathrm{C}_{n}$ or
$-\mathrm{dC} / \mathrm{C}_{n}=\mathrm{kdt}$
$-\mathrm{C}-\mathrm{ndC}=\mathrm{kdt}$
$-\left[C^{-n+1} /-n+1\right] c^{C 0}=k t$
$1 / n-1\left[1 / C^{n-1}-1 / C_{0}^{n-1}\right]=k t$

For a second order reaction,
$k=1 / t\left(1 / C-1 / C_{0}\right)$
If $\mathrm{C}_{0}$ is a , and C is $\mathrm{a}-\mathrm{x}$
$k=1 / t(1 / a-x-1 / a)=1 / t[x /(a-x) a]$
Let us consider,
A $+B \rightarrow$ Products
$-d C_{A} / d t=-d C_{B} / d t=k C_{A C B}$
If $a$ and $b$ represents initial moles of $A$ and $B$ and $x$ represents the amount of each that has reacted after time $t$, $d x / d t=k(a-x)(b-x)$
If $a=b$ i.e. $A$ and $B$ are present in equimolar
amounts, $\mathrm{dx} / \mathrm{dt}=\mathrm{k}(\mathrm{a}-\mathrm{x})_{2}=\mathrm{k}(\mathrm{b}-\mathrm{x})_{2}$
Integration of (1) yields (by the method of partial functions).
$k=[1 / t(a-b)] \ln [b(a-x) / a(b-x)]$

The rate constant depends upon the units employed to express concentrations.
The units of $k$ are con-1 time-1. If the concentration is moles/litre, k will be (moles/litre).-1 sec-1
$k=1 / t(x / a(a-x))$
When x is $\mathrm{a} / 2$,
to. $5=1 /$ ka, the time is inversely proportional to initial concentration, in sharp difference with the first order reactions. For any other fraction, a similar relation exists.

## Examples

The decomposition of HI is a second order reaction. However, the study of this reaction is difficult since the reaction is reversible.
One reaction that is second order is $\mathrm{H}_{2}+\mathrm{C}_{2} \mathrm{H}_{4}=\mathrm{C}_{2} \mathrm{H}_{6}$.
The reaction can be studied by determining the pressure at various times.
Reaction of isobutyl bromide and sodium ethoxide is second order.
$\mathrm{C}_{4} \mathrm{HgBr}+\mathrm{OEt}^{-} \rightarrow \mathrm{C}_{4} \mathrm{HgOE}+\mathrm{Br}^{-}$

## Saponification of an ester is a second order reaction.

$\mathrm{CH}_{3} \mathrm{COOC}_{2} \mathrm{H}_{5}+\mathrm{OH}^{-}=\mathrm{CH}_{3} \mathrm{COO}^{-}+\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{OH}$
This is different from the acid hydrolysis since both reactants are present in similar amounts.

The reaction can be studied by a number of methods. The first method is by conductance measurements. The replacement of OH - ions by $\mathrm{CH}_{3} \mathrm{COO}$ - ions will change the conductance of the solution. This change can be correlated with the extent of the reaction.
In the second, definite quantities of the reaction mixture are withdrawn at intervals and the amount of alkali left out is determined. If the initial concentrations of alkali and ester are known, the rate constant can be determined.

Rate can also be treated graphically.
$t=[2.030 / k(a-b)] \log b / a+[2.303 / k(a-b)] \log a-x / b-x$
Plot of $t$ against $\log [a-x / b-x]$ will give a straight line with slope [2.303/k(a-b)]
Reactions of alkyl iodides with tertiary amines is also second order.
$\mathrm{C}_{2} \mathrm{H}_{5} \mathrm{I}+\mathrm{C}_{6} \mathrm{H}_{5} \mathrm{~N}\left(\mathrm{CH}_{3}\right)_{2} \rightarrow \mathrm{C}_{6} \mathrm{H}_{5} \mathrm{~N}\left(\mathrm{CH}_{3}\right)_{2} \mathrm{C}_{2} \mathrm{H}_{5}{ }^{+}+\mathrm{I}-$

## Third order reactions

$A+B+C \rightarrow$ Products
$2 A+B \rightarrow$ Products
3A $\rightarrow$ Products
$-\mathrm{dC} / \mathrm{dt}=\mathrm{kC}_{3}$
$K=1 /(2 t)\left(1 / C^{2}-1 / C_{0}^{2}\right)$
$=1 /(2 \mathrm{t})[(1 /(\mathrm{a}-\mathrm{x}) 2-1 / \mathrm{a} 2]$
Unit con-2 time-1
For order $n$, $k$ is conc. $n-1$ time-1
For completing half of the reaction,
$k=1 /(2 t) 3 / a 2$
$\mathrm{t}_{0} .5=3 /\left(2 \mathrm{ka}^{2}\right)$

Time to complete a fraction is inversely proportional to the square of the initial concentration.

There are five gas phase reactions which are definitively third order. These are the termolecular reactions involving two molecules of nitric oxide and one molecule of $\mathrm{Cl}_{2}, \mathrm{H}_{2}, \mathrm{D}_{2}, \mathrm{O}_{2}$ or $\mathrm{Br}_{2}$.
$2 \mathrm{NO}+\mathrm{Cl}_{2}=2 \mathrm{NOCl}$
For reactions of the type,
$2 \mathrm{~A}+\mathrm{B} \rightarrow$ Products
If $x$ is the amount of $B$ reacted after time $t$, $d x / d t=k(a-2 x) 2(b-x)$
$k=1 / t(2 b-a) 2[(2 b-a) 22 x / a(a-2 x)+\ln [b(a-2 x) / a(b-x)]]$
Although a number of third order reactions in solution are reported, none of them is proven.

Complications and how to solve them

1. Pseudo Order

An expression for second order reaction $2 \mathrm{~A} \rightarrow$ Products
Can be written as,
$-\mathrm{dA} / \mathrm{dt}=\mathrm{k}[\mathrm{A}]_{2}$
And the integration,
$\int-1 / A_{2} d A=k d t$
$1 / A_{t}-1 / A_{o}=k t$
This integration is rather easy. The amount of reactant present at any time can be calculated knowing k.

## Look at the expression, $-\mathrm{dA} / \mathrm{dt}=\mathrm{k}[\mathrm{A}][\mathrm{B}]$

is not very easy. If there is a relation between the concentration of $A$ and $B$, an expression could be derived since, $d A / d t=d(A-$ $\mathrm{x}) / \mathrm{dt}=-\mathrm{dx} / \mathrm{dt}$
$d x / d t=k(A) t(B) t=k(A-x)(B-x)$
Integrating
$k t=\left[1 / A_{0}-B_{0}\right] \ln \left[\left(A_{t}\right)\left(B_{0}\right) /\left(A_{0}\right)(B) t\right]$
This kind of expressions gets complicated as the relation between compositions of the reacting species gets complex.

Simplification by Ostwald's isolation method.

This depends on the approximation that when the reactant is present in large excess, the concentration is hardly changed during the course of the reaction.
$-d A / d t=k[A][B]$ gets reduced to $-d A / d t=k^{\prime}[A]$
when $B$ is present in large excess or $B_{0} \approx B_{t}$.
This is the pseudo first order rate law.
The third order rate law, $-\mathrm{dA} / \mathrm{dt}=\mathrm{k}\left[\mathrm{A}_{2}\right][\mathrm{B}]$
Reduces to pseudo first order, if $A$ is present in excess.

If $B$ is in excess, it becomes pseudo second order.

## 2. Reactions occur in stages

Third order reactions are hard to occur.
Higher order reactions (more than three) are very rare, may not even occur.

Reasons: Geometry, orientation,...

## INTERMEDIATE

Then how is that third order reactions are occurring?
The fact that in all of the third order reactions NO is an ingredient seems to suggest that an intermediate reagent involving NO is taking part. The dimer of $\mathrm{NO},(\mathrm{NO})_{2}$ is long-lived. Thus it can take part in the reaction like, $(\mathrm{NO})_{2}+\mathrm{Cl}_{2}=2 \mathrm{NOCl}$
The reaction is kinetically third order since rate dependence on the square of the NO concentration.

# Concept of intermediate <br> Valid in solutions also 

Reactions may happen in steps!
This simplifies equations.

The reaction of NO and $\mathrm{H}_{2}$ forming $\mathrm{N}_{2}$ and $\mathrm{H}_{2} \mathrm{O}$ seems to occur in two states.

$$
2 \mathrm{NO}+2 \mathrm{H}_{2}=\mathrm{N}_{2}+2 \mathrm{H}_{2} \mathrm{O}
$$

The steps appear to be,

$$
\begin{aligned}
& 2 \mathrm{NO}+\mathrm{H}_{2} \rightarrow \mathrm{~N}_{2}+\mathrm{H}_{2} \mathrm{O}_{2} \text { (Slow) } \\
& \mathrm{H}_{2} \mathrm{O}_{2}+\mathrm{H}_{2} \rightarrow 2 \mathrm{H}_{2} \mathrm{O} \text { (Fast) }
\end{aligned}
$$

$\rightarrow$ Indicates intermediate stage although the exact nature of the intermediate steps is not clear, it appears that one step involves 2 NO and $\mathrm{H}_{2}$.

In the case of a complex reaction, the rate is determined by the slowest process.

It could be any one of the steps.
All the kinetic studies have shown that even for the moderately complex reactions, the reaction occurs in stages. The stoichiometric reaction does not always represent the true reaction.

How do you find slowest step? Mechanism.
Check out..
Hydrolysis of an ester in dilute acid medium. The reaction
rate is independent of the anion for strong acids. This shows that the hydrolysis of the ester is essentially catalysed by protons.

Thus one can write the first probable reaction.
(1) $\mathrm{RCOOR}{ }^{\prime}+\mathrm{H}_{+}=\mathrm{R}-\mathrm{CO}-\mathrm{OH}+-\mathrm{R}^{\prime}$ (fast)

At any acid concentration, the rate depends only on the concentration of the ester. Thus one can say that the equilibrium lies to the left.
Otherwise the acidity decreases upon addition of further acid.
We know that the reaction is first order in both the ester and the acid.
We suggest the following mechanism,
(2) $\mathrm{R}-\mathrm{CO}^{-}-\mathrm{OH}^{+}-\mathrm{R}^{\prime}+\mathrm{H}_{2} \mathrm{O}=\mathrm{R}-\mathrm{CO}-\mathrm{OH}_{2}{ }^{+}+\mathrm{R}^{\prime} \mathrm{OH}$ (slow)
the reaction involves the breakage of covalent $\mathrm{O}-\mathrm{R}^{\prime}$ bond.
This is slow. The next step involves the regeneration of acid,
since it is a catalyst.
(3) $\mathrm{R}-\mathrm{CO}-\mathrm{OH}_{2+}=\mathrm{RCOOH}+\mathrm{H}_{+}$(fast)

This reaction almost goes to completion. In these steps it can be seen that step 2 is the rate limiting step.

Summary: Reactions can be tested.

## 3. Determination of the order of reactions

## Method of trial

Order of the reaction is the one corresponding to the best formula.
Graphical method can be adopted if data at number of time intervals is available.
For first order, $t=$ constant $-(2.303 / k) \log c$
For order, $n \quad t=$ constant $+[1 / k(n-1)] 1 / c_{n-1}$
Plot of t vs. $1 / \mathrm{cn}$-1 should give a straight line. $1 / \mathrm{c}$ for second and $1 / \mathrm{c} 2$ for third.

## Time to complete a definite fraction of the reaction

For a reaction of order $n$, the time to complete half the
Reaction, $\mathrm{t} 0.5=$ constant * $1 / \mathrm{co}^{\mathrm{n}-1}$
Time required to decompose half the reactants is constant for first order. In general it is proportional to $1 / \mathrm{c}_{\mathrm{n}-1}$. In other words to. $5 \mathrm{x} \mathrm{co}^{\mathrm{n}-1}$ is a constant.

By varying the initial concentration of the reactants and measuring the time taken for a definite function to decompose, one can determine the order.

## Differential method

$-\mathrm{dc} 1 / \mathrm{dt}=\mathrm{kc} 1 \mathrm{n} \quad-\mathrm{dc} 2 / \mathrm{dt}=\mathrm{kc} 2 \mathrm{n}$
Where $\mathrm{c}_{1}$ and $\mathrm{c}_{2}$ are two different concentrations of the
reactants. Take log and subtract
$\mathrm{n}=[\log (-\mathrm{dc} 1 / \mathrm{dt})-\log (-\mathrm{dc} 2 / \mathrm{dt})] /\left[\log c_{1}-\log \mathrm{c}_{2}\right]$
$\mathrm{dc} / \mathrm{dt}$ and $\mathrm{dc} / \mathrm{dt}$ can be determined by plotting con. c against time and taking slope (dc/dt) at two different concentrations. Plot of log(-dc/dt) against $\log (\mathrm{c})$ gives n . Alternatively one can determine -dc/dt at two concentrations and insert in the equation. The results are independent of concentration units if all are expressed similarly.

## 4. Opposing Reactions

Reactions may proceed to a state of equilibrium which differs appreciably from completion. The simplest case of this occurs when both forward and reverse reactions are of the first order, so that the situation can be represented as,


Assume that k 1 and $\mathrm{k}-1$ are the rate constants in the forward and reverse directions. If the experiment is started using pure A , of concentration a0, and if after the time $t$ the concentration of X is x , then that of A is
$\mathrm{a}_{0}-\mathrm{x}$. The net rate of production of X is,

$$
\begin{equation*}
d x / d t=k_{1}(a 0-x)-k-1 x \tag{1}
\end{equation*}
$$

$X$ is being produced by the forward reaction (first term) and removed by the reverse reaction (second term). If $X_{e}$ is the concentration of $X$ at equilibrium, when the net rate of reaction is zero,

$$
\begin{align*}
& 0=k_{1}\left(a_{0}-x_{e}\right)-k_{-1} x_{e}  \tag{2}\\
& k_{-1}=k_{1}\left(a_{0}-x_{e}\right) / x_{e}
\end{align*}
$$

Substitution of this expression in Eq. (1) gives rise to,

$$
d x / d t=\left(k 1 a 0 / x_{e}\right)\left(x_{e}-x\right)
$$

Integration of this equation, using the fact that $\mathrm{x}=0$ when $\mathrm{t}=0$, gives

$$
\begin{equation*}
\mathrm{k}_{1}=\mathrm{xe}_{\mathrm{e}} / \mathrm{aot}\left[\ln \mathrm{xe}_{\mathrm{e}} /\left(\mathrm{x}_{\mathrm{e}}-\mathrm{x}\right)\right] \tag{3}
\end{equation*}
$$

If $x_{e}$ is known, it is possible to calculate $\mathrm{k}_{1}$ from measurements of x as a function of the time.
For certain purposes it is convenient to have this equation in a different form.
From (2),

$$
\begin{aligned}
& x_{e}\left(k_{1}+k_{-1}\right)=k_{1} a_{0} \\
& x_{e} / a_{0}=k_{1} /\left(k_{1}+k_{-1}\right)
\end{aligned}
$$

Equation (3) may therefore be written as

$$
k_{1}=k_{1} /\left(k_{1}+k_{-1}\right) 1 / t \ln x_{e} /\left(x_{e}-x\right)
$$

or

$$
\begin{equation*}
k_{1}+k_{-1}=1 / t \ln x_{e} /\left(x_{e}-x\right) \tag{4}
\end{equation*}
$$

Comparison of this equation with that for a simple first-order reaction shows that the two are formally analogous, $\mathrm{xe}_{\mathrm{e}}$ replacing a 0 , and $\mathrm{k}_{1}+\mathrm{k}$ 1 replacing k .

Here it has been assumed that the initial concentration of the product $X$ is zero. If this is not the case, and the initial concentrations of $A$ and X are a 0 and xo , the net rate at time t is given by,

$$
d x / d t=k_{1}\left(a_{0}-x\right)-k-1\left(x+x_{0}\right)
$$

By methods similar to those used earlier it can be shown that this equation integrates to

$$
k_{1}+k_{-1}=1 / t \ln \left[\left(k_{1} a 0-k-1 x_{0}\right) /\left(k_{1} a_{0}-k_{-1} \times 0-\left(k_{1}+k_{-1}\right) \mathrm{x}\right)\right](5)
$$

The concentration $\mathrm{x}_{\mathrm{e}}$, at equilibrium, is defined by

$$
x_{e}=\left(k_{1} a_{0}-k_{-1} x_{0}\right) /\left(k_{1}+k_{-1}\right)
$$

Equation (5) reduces to

$$
\mathrm{k}_{1}+\mathrm{k}_{-1}=1 / \mathrm{ln} \mathrm{x}_{\mathrm{e}} /\left(\mathrm{x}_{\mathrm{e}}-\mathrm{x}\right)
$$

which is the same as Eq. (4)

## RATE EQATIONS FOR OPPOSING REACTIONS

| Stoichiometric equation | Rate equation | Integrated rate equation |
| :---: | :---: | :---: |
| $A \equiv X$ |  |  |
| $A \equiv X$ | $d x / d t=k_{1}\left(a_{0}-x\right)-k_{-1}\left(x+x_{0}\right)$ | $x_{e} / a_{0} \ln x_{e} / x_{e}-x=k_{1} t$ |
| $2 A \equiv X$ | $d x / d t=k_{1}\left(a_{0}-x\right)-{ }_{-1} \mathrm{x} / 2$ |  |
| $A \equiv 2 X$ | $d x / d t=k_{1}\left(a_{0}-x / 2\right)-k_{-1}$ |  |
| $A \equiv X+Y$ | $\mathrm{dx} / \mathrm{dt}=\underset{1}{\mathrm{k}}(\mathrm{a}-\mathrm{x})-\mathrm{k} \mathrm{x}_{-1} \mathrm{x} 2$ |  |
| $A+B \equiv X$ | $\mathrm{dx} / \mathrm{dt}=\underset{1}{\mathrm{k}}(\mathrm{a}-\mathrm{x})_{2}-\mathrm{k} \mathrm{x}_{-1}$ |  |
| $A+B \equiv X+Y$ | $\mathrm{dx} / \mathrm{dt}=\underset{\mathrm{k}}{\mathrm{k}}\left(\begin{array}{lll} (\mathrm{a} & -\mathrm{x})_{2}-\mathrm{k} & \mathrm{x} 2 \\ -1 \end{array}\right.$ |  |
| $2 A \equiv X+Y$ | $\mathrm{dx} / \mathrm{dt}=\mathrm{k}_{1}\left(\mathrm{a}_{0}-\mathrm{x}\right)^{2}-\mathrm{k}{\underset{-1}{ }(\mathrm{x} / 2)_{2} 2}^{2}$ <br> CY101 2007 | radeep |

## 5. Parallel Reactions

These reactions are those in which the reacting molecules convert through more than one channel yielding different sets of products. The reaction resulting in the product is known as the main or the major reaction and the other reactions are referred to as side or parallel reactions. To calculate the overall rate, the rate of the side reactions should be taken into account. Consider a reaction,


The rates these two reactions are, and

$$
d[B] / d t=k_{1}[A]
$$

$$
d[C] / d t=k^{\prime}[[A]
$$

The overall rate of disappearance of $A$ is given

$$
\begin{align*}
\text { by }-\mathrm{d}[\mathrm{~A}] / \mathrm{dt} & =\mathrm{k}_{1}[\mathrm{~A}]+\mathrm{k}^{\prime} 1[\mathrm{~A}] \\
& =\left[\mathrm{k}_{1}+\mathrm{k}^{\prime} 1\right][\mathrm{A}] \tag{1}
\end{align*}
$$

The ratio of the two rates is given as

$$
\begin{equation*}
\mathrm{d}[\mathrm{~B}] / \mathrm{dt} / \mathrm{d}[\mathrm{C}] / \mathrm{dt}=\mathrm{k}_{1} / \mathrm{k}^{\prime} 1 \tag{2}
\end{equation*}
$$

With the help of these equations (1 and 2), the rate constants for individual steps can be calculated.

An example of parallel reaction is the nitration of phenol.


The parallel reaction depicted above can get complicated. In the situation below, if $\mathrm{k}^{\prime \prime} 1$ is large in comparison to $\mathrm{k}^{\prime} 1$, all the C formed will become D immediately.


Therefore, the set of reactions actually will be just as the kind written in the beginning, instead of C , the product observed will be D . If k 1 and $\mathrm{k}^{\prime} 1$ have similar magnitude, amount of $A$ and $D$ formed will be the similar.

## Equilibrium constant and specific reaction rate

 $\mathrm{K}=\mathrm{k} / \mathrm{k}^{\prime}$This relation is already implied in, $k\left(a-x_{e}\right)=k^{\prime} x_{e}$
This values of $k$ and $k$ derived from this equation cannot be used to calculate K. In general the values of k and $\mathrm{k}^{\prime}$ can be determined by studying the rates of forward and backward reactions in the early states when the opposing reaction is negligible. The value of K can be determined by analysing the reacting system at equilibrium. The equilibrium constant determined from and $k$ and $k$ ' may not exactly correspond with the true equilibrium constant. In the esterification of acetic acid by ethanol, if one wants to determine the equilibrium constant, first k for the forward reaction is measured assuring that the backward reaction is negligible. Similarly, the forward reaction rate constant of the hydrolysis of ethyl acetate is determined under identical conditions. Here again the reverse reaction is neglected. The equilibrium constant calculated, as the ratio of these rate constants vary slightly from the true value determined from the concentration.

